

The Matrix



What is a matrix?

A Matrix is an array of numbers in Rows and Columns.

$$\begin{bmatrix} 3 & -2 \\ 4 & 0 \\ -1 & 5 \end{bmatrix}$$

This is a 3x2 matrix containing 6 elements.

Vocabulary

- Dimensions of a Matrix - given by #rows x # columns
- Elements/Entries - the numbers in a matrix
- Equal Matrices - two matrices are equal if their dimensions are the same and their corresponding entries are equal.

$$\begin{bmatrix} -1 & 1/2 \\ -2 & 0 \end{bmatrix} = \begin{bmatrix} -1 & .5 \\ 2 & 0 \end{bmatrix}$$

Vocabulary

- Row Matrix - a matrix with only one row $[-1 \ 4 \ 0]$
- Column Matrix - a matrix with only one column $\begin{bmatrix} 3 \\ -2 \\ 1 \\ 5 \end{bmatrix}$
- Square Matrix - a matrix with the same number of rows as columns

$$\begin{bmatrix} 5 & 0 \\ -3 & -4 \end{bmatrix}$$

Scalar Multiplication

To multiply a matrix by a scalar, multiply each entry in the matrix by the scalar.

$$\text{Ex. } 2 \begin{bmatrix} 5 & 0 \\ -3 & -4 \end{bmatrix}$$

Solving Matrix Equations

If two matrices are equal, their corresponding entries are equal.

$$\text{Ex. } \begin{bmatrix} x & 1 \\ -3 & y \end{bmatrix} = \begin{bmatrix} 5 & 1 \\ -3 & -6 \end{bmatrix}$$

Adding Matrices

To add matrices, add corresponding entries.

$$\text{Ex. } \begin{bmatrix} 3 & -2 \\ 4 & 0 \\ -1 & 5 \end{bmatrix} + \begin{bmatrix} 1 & 4 \\ -7 & 3 \\ -5 & 1 \end{bmatrix}$$

Subtracting Matrices

To subtract matrices, subtract corresponding entries.

$$\text{Ex. } \begin{bmatrix} 3 & -2 \\ 4 & 0 \\ -1 & 5 \end{bmatrix} - \begin{bmatrix} 1 & 4 \\ -7 & 3 \\ -5 & 1 \end{bmatrix}$$